

(8)

1st reminder of iterative method Gauss-Seidel

to solve $Ax = b$

one iteration, i.e. we have $x^{(k)}$ and get $x^{(k+1)}$ for $i = 1:n$

$$x_i^{(k+1)} = \frac{b_i - \sum_{j < i} a_{ij} x_j^{(k+1)} - \sum_{j > i} a_{ij} x_j^{(k)}}{a_{ii}}$$

and

we do this several iterations till $\|x^{(k+1)} - x^{(k)}\|$ is very small.

Gauss-Seidel for the Crank Nicolson system $\otimes$ (European)

$$b_1 = \kappa_1 (f_0^n + f_0^{n-1}) + (1 + \beta_1) f_1^n + \gamma_1 f_2^n$$

$$b_i = \kappa_i f_{i-1}^n + (1 + \beta_i) f_i^n + \gamma_i f_{i+1}^n \quad 2 \leq i \leq M-2$$

$$b_{M-1} = \kappa_{M-1} f_{M-2}^n + (1 + \beta_{M-1}) f_{M-1}^n + \gamma_{M-1} (f_M^n + f_M^{n-1})$$

recall κ_i, β_i & γ_i

$$a_{ii-1} = -\kappa_i \quad 2 \leq i \leq M-1$$

$$a_{ii} = (1 - \beta_i) \quad 1 \leq i \leq M$$

$$a_{ii+1} = -\gamma_i \quad 1 \leq i \leq M-2$$

$$a_{ij} = 0 \quad \text{if} \quad |j - i| \geq 2$$